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**Addendum and errata “Hyperbolic tessellations,  
modular symbols, and elliptic curves over  
complex quadratic fields”**

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## Addendum and errata

### Hyperbolic tessellations, modular symbols, and elliptic curves over complex quadratic fields

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#### Addendum

On page 315 of the original paper [1], a table of twelve “missing conductors” was given. These were ideals  $\mathfrak{f}$  for which we expected to find an elliptic curve with conductor  $\mathfrak{f}$  and certain specific traces of Frobenius, as predicted by the Main Conjecture on page 298, but had not yet found such a curve. Twelve such curves have now been found, and, in Table 1, we give their details to complete the tables in [1]. (We reiterate that the tables of curves in [1] are not closed under isogeny.) For each curve, we give its conductor  $\mathfrak{f}$ , and the coefficients  $a_1, a_2, a_3, a_4$  and  $a_6$  of a minimal Weierstrass equation.

In the case of  $\mathfrak{f} = (17 + 11i)$ , the curve above corresponds to the first newform in  $V^+(17 + 11i)$  listed in Table 3.2.2 of [1]; a curve corresponding to the second newform was already given in Table 3.2.3.

Table 1.

Field	$\mathfrak{f}$	$a_1$	$a_2$	$a_3$	$a_4$	$a_6$
$\mathbf{Q}(i)$ ( $i = \sqrt{-1}$ )	$(17 + 11i)$	-1	$-1 - i$	$-i$	$55 - 67i$	$-31 + 57i$
	$(19 + 8i)$	$1 + i$	$-1 - i$	1	$-19 + 4i$	$-4 + 13i$
$\mathbf{Q}(\theta)$ ( $\theta = \sqrt{-2}$ )	$(6 + 6\theta)$	$\theta$	$1 - \theta$	$\theta$	$4 - 3\theta$	$4 - 2\theta$
	$(5 + 10\theta)$	$\theta$	-1	$1 + \theta$	$2 - 3\theta$	$5 - \theta$
	$(12 + 7\theta)$	$-1 - \theta$	$\theta$	-1	$13 + 9\theta$	$40 + 10\theta$
$\mathbf{Q}(\varrho)$ ( $\varrho = \frac{1}{2}(1 + \sqrt{-3})$ )	$(3 + 12\theta)$	$\theta$	$1 - \theta$	$1 + \theta$	$-3\theta$	$1 - 2\theta$
	$(14 + 7\varrho)$	$1 - \varrho$	$1 - \varrho$	$-\varrho$	$11 - 7\varrho$	$-5 - 9\varrho$
	(21)	-1	-1	$-\varrho$	$-3 + 4\varrho$	$1 - 4\varrho$
$\mathbf{Q}(\alpha)$ ( $\alpha = \frac{1}{2}(1 + \sqrt{-7})$ )	(14)	-1	$-2 + \alpha$	$-\alpha$	$-10 + \alpha$	$-8 - \alpha$
$\mathbf{Q}(\alpha)$ ( $\alpha = \frac{1}{2}(1 + \sqrt{-11})$ )	$(6\alpha)$	$1 - \alpha$	$-1 - \alpha$	$-\alpha$	$-9 + 5\alpha$	$15 - 2\alpha$
	$(2 + 7\alpha)$	$1 + \alpha$	$\alpha$	$1 + \alpha$	$-4 + \alpha$	-3
	$(6 + 6\alpha)$	$\alpha$	$-1 - \alpha$	0	4	0

Thanks are due to R.G.E. Pinch, who found the curves with  $\mathbf{f} = (3 + 12\theta)$  and  $\mathbf{f} = (2 + 7\alpha)$ . The rest were found by the author using programs written in Algol68, run on the ICL 2980 computer at the South West Universities Regional Computing Centre.

### *Errata*

– Table 3.2.3: The line with  $\mathbf{f} = (16)$  should have a  $\sqrt{\quad}$  in the column headed “CM(1)?”.

– Table 3.5.2: The line with  $\mathbf{a} = (3 - 6\alpha)$  should read

$$(3 - 6\alpha) - 1 - 1 + - 4 \ 4 \ 0 \ 0 \ -6 \ -2 \ -2 \ 6 \ 6 \ -4 \ -4$$

– Table 3.5.3: The four lines with  $\mathbf{f} = (8\alpha)$  should be linked in the last column (by 2-isogenies).

### **References**

1. J.E. Cremona: Hyperbolic tessellations, modular symbols, and elliptic curves over complex quadratic fields. *Comp. Math.* 51 (1984) 275–323.